

Solving by Elimination

- When neither equation is arranged in the form $y =$ or $x =$, a third method of solving is needed: elimination.
- This method eliminates one of the variables by either adding or subtracting the two equations together.
- Identify the coefficient that is the same in both equations, then examine its sign. The rule is SAME SIGN SUBTRACT!

Ex/ Solve.

a) $\begin{cases} 2x + 4y = 9 \\ 2x + 3y = 4 \end{cases}$

Same terms
and
same signs
so subtract

$$\begin{aligned} 1y &= 5 \\ y &= 5 \end{aligned}$$

Pick one of original
 $2x + 3y = 4$

multiply
numbers on one
side, letters on
the other

$$\begin{aligned} 2x + 3(5) &= 4 \\ 2x + 15 &= 4 \end{aligned}$$

$$\begin{aligned} 2x &= 4 - 15 \\ 2x &= -11 \\ \frac{2x}{2} &= \frac{-11}{2} \\ x &= -5.5 \end{aligned}$$

POI
 $(-5.5, 5)$

b) $\begin{cases} 3x + 2y = 5 \\ x - 2y = -1 \end{cases}$

same terms
but opposite signs
so Add

$$\begin{aligned} 4x &= 4 \\ x &= 1 \end{aligned}$$

$$\begin{aligned} x - 2y &= -1 \\ 1 - 2y &= -1 \\ -2y &= -1 - 1 \\ -2y &= -2 \\ \frac{-2y}{-2} &= \frac{-2}{-2} \\ y &= 1 \end{aligned}$$

POI $(1, 1)$

If no coefficients are equal, multiply the whole equation by a constant (make an equivalent equation)

c) $\begin{cases} 3x + 2y = 5 \\ 3x - 6y = -1 \end{cases}$

Add

$$\begin{aligned} -4y &= 4 \\ y &= -1 \end{aligned}$$

$$\begin{aligned} 3x - 6y &= -1 \\ 3x - 6(-1) &= -1 \\ 3x + 6 &= -1 \\ 3x &= -1 - 6 \\ 3x &= -7 \\ \frac{3x}{3} &= \frac{-7}{3} \\ x &= -\frac{7}{3} \end{aligned}$$

POI
 $(-\frac{7}{3}, -1)$

doesn't divide
nicely so just
leave

d) $2x + 5y = 4$

$\rightarrow (-x + 3y = 9)$ multiply whole thing by 2

Add $\begin{cases} 2x + 5y = 4 \\ -2x + 6y = 18 \end{cases}$

$$\begin{aligned} 2x + 5y &= 4 \\ 2x + 5(2) &= 4 \\ 2x + 10 &= 4 \\ 2x &= 4 - 10 \\ 2x &= -6 \\ \frac{2x}{2} &= \frac{-6}{2} \\ x &= -3 \end{aligned}$$

POI $(-3, 2)$

Same sign subtract

$$\begin{array}{rcl} \text{e) } 3x + 2y & = & 1 \\ 2x + 4y & = & -2 \\ \hline 6x + 4y & = & 2 \end{array}$$

multiply by 2

$$\begin{array}{r} -4x = -4 \\ \hline -4 \quad -4 \end{array}$$

$$x = 1$$

$$\text{POI } (1, -1)$$

$$2x + 4y = -2$$

$$2(1) + 4y = -2$$

$$2 + 4y = -2$$

$$4y = -2 - 2$$

$$\frac{4y}{4} = \frac{-4}{4}$$

$$y = -1$$

Ex/ Four chocolate bars and three ice-cream cones cost \$5.30. Two chocolate bars and one ice-cream cone cost \$2.20. Find the cost of a chocolate bar and the cost of an ice-cream cone.

$$4b + 3c = 5.30$$

$$2b + c = 2.20 \leftarrow \text{multiply by 3}$$

Subtract

$$\begin{array}{rcl} 4b + 3c & = & 5.30 \\ 6b + 3c & = & 6.60 \\ \hline \end{array}$$

$$\begin{array}{r} -2b = -1.30 \\ \hline -2 \quad -2 \end{array}$$

$$b = 0.65$$

$$2b + c = 2.20$$

$$2(0.65) + c = 2.20$$

$$1.3 + c = 2.20$$

$$c = 2.20 - 1.30$$

$$c = 0.9$$

\therefore Bars cost \$0.65 and cones \$0.90

Practice: Handout - Solving by Elimination